



- 3) A stationary time series is _____ if $\gamma(h) = 0$ whenever $|h| > q$.
- 4) A sequence of uncorrelated random variables, each with zero mean and variance σ^2 is called _____
- 5) The Spencer 15-point moving average is a filter that passes polynomials upto degree _____ without distortion.
- C) State whether the following statements are **true** or **false** : **4**
- 1) The random walk is a weak stationary process.
 - 2) Every IID noise is white noise.
 - 3) Every white noise is IID noise.
 - 4) The autocorrelation function $\gamma(h)$ is symmetric in h .
2. a) i) Define Ar(p) Process. Find its Autocorrelation Function (ACF).
 ii) Define an invertible process. Give one example. **(3+3)**
- b) Write short note on the following :
 i) Double exponential smoothing.
 ii) Weak and strict stationarity. **(4+4)**
3. a) Define a causal process. State conditions under which an ARMA process is causal. Examine whether the process $X_t + 1.6 * X_{t-1} = Z_t - 0.4 * Z_{t-1}$ is causal.
 b) Define MA(q) process. Obtain its autocovariance function. **(7+7)**
4. a) What do you mean by smoothing of a time series ? Also explain Holt-Winter exponential smoothing.
 b) Describe the main components of time series. Discuss any one method of trend removal in the absence of a seasonal component. **(6+8)**
5. a) Describe the need of ARCH and GARCH models.
 b) Define the ARIMA model. Discuss the problem of forecasting ARIMA models. **(6+8)**
6. a) Describe the test based on turning points for testing randomness of residuals.
 b) For the model $(1 - 0.2 B) X_t = (1 - 0.5 B) Z_t$, evaluate the first three π -weights and the first three ψ -weights. **(6+8)**
7. a) Discuss in brief about Yule-Walker equations.
 b) Describe Durbin-Levinson algorithm for fitting AR(p) model. **(6+8)**
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B) Fill in the blanks : 5

- 1) $\{X_t\}$ is a _____ stationary time series if (X_1, \dots, X_n) is identical in distribution with $(X_{1+h}, \dots, X_{n+h})$ for all integers h and $n \geq 1$.
- 2) If mean and covariance function are both independent of time t , then the process is called _____ stationary.
- 3) A white noise sequence is _____ stationary.
- 4) A real-valued function defined on the integers is the autocovariance function of a stationary time series if and only if it is even and _____
- 5) The MA(1) process is _____ stationary.

C) State whether the following statements are **true** or **false** : 4

- 1) Weak stationarity implies strict stationarity.
- 2) A process $\{X_t\}$ is invertible, if Z_t can be expressed in terms of the present and past values of the process $X_s, s \leq t$.
- 3) ARCH model is used to describe a changing, possibly volatile variance.
- 4) The random walk is a weak stationary process.

2. a) Define PACF of a process $\{X_t\}$. Find an expression for PACF of the following process

$$X_t = 0.5 X_{t-1} + Z_t, Z_t \sim \text{iid } N(0, \sigma^2) \quad \text{8}$$

- b) i) State any two properties of white noise process.
- ii) Define an invertible process. Give one example. (3+3)

3. a) Explain moving average smoothing. Describe forecasting based on smoothing.

b) Define an ARMA(p, q) process and state conditions for its invertibility. Examine the process $X_t - 0.5X_{t-1} + 0.3 X_{t-2} = Z_t + 0.2 Z_{t-1}$ for invertibility. (7+7)



4. a) Define MA(q) process. Obtain its autocovariance function.
b) What are the different methods of diagnostic checking in time series ?
Explain the role of residual analysis in model checking. **(7+7)**
 5. a) Describe Yule-Walker method of estimating the parameters of an AR(p) process. Obtain the same for AR(2) process.
b) Obtain the autocorrelation function of a stationary AR(1) process. **(6+8)**
 6. a) Explain the concept of spectral density of a time series. Derive the spectral density of an AR(1) process.
b) Describe the main components of time series. Discuss any one method of trend removal in the absence of a seasonal component. **(8+6)**
 7. a) Discuss recursive prediction of an ARMA (p, q) process.
b) Outline a procedure for model selection of an observed time series. **(7+7)**
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